

### Intracluster medium contd..

- The ICM in addition to being at thermal equilibrium, is also in hydrostatic (Pressure) equilibrium. This means that any disturbance created in the medium is propagated at the speed of sound. So the travel time of sound to the outer edge of the cluster will give an estimate of the timescale in which it achieves equilibrium

$$t_p = \frac{R}{C_s} \quad (1)$$

$$t_p = \frac{Mpc}{\sqrt{\frac{\gamma K t}{\mu m_H}}} \quad (2)$$

- Therefore,

$$t_p = 6.5 \times 10^8 \times \frac{T^{-0.5}}{10^{-4}} \times \frac{D}{Mpc} \quad (3)$$

### An estimate of mass

- The condition for Hydrostatic Equilibrium will give the Mass enclosed within a radius  $r$  provided that the density and temperature profile are known.

$$\frac{dp}{dr} = -\frac{GM(r)}{r^2} \quad (4)$$

- From the ideal gas equation,  $\frac{dp}{dr}$  can be expressed in terms of  $\frac{d\rho}{dr}$

$$\frac{dp}{dr} = \frac{KT}{\mu M_H} \times \left( T \frac{d\rho}{dr} + \rho \frac{dT}{dr} \right) = -\frac{GM(r)}{r^2} \quad (5)$$

- Finally,

$$M(r) = \frac{KT}{\mu G m_H} \left( \frac{d \ln \rho}{d \ln r} + \frac{d \ln T}{d \ln r} \right) r \quad (6)$$



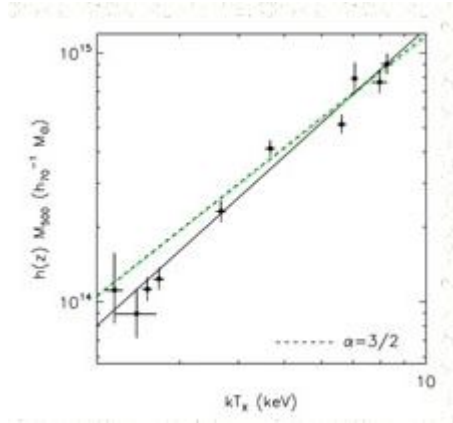


Figure 2: The mass - temperature relation of a sample of regular clusters

### Virial Temperature

- Virial temperature corresponding to gravitational potential energy which keeps the gas at  $10^8\text{K}$  bound together i.e it does not reach escape velocity

$$\frac{\mu m_H \sigma^2}{2} = \frac{3K_B T_{vir}}{2} \quad (7)$$

$$T_{vir} = \frac{\mu m_H \sigma^2}{3K_B} \quad (8)$$

- For an isothermal sphere of gas,

$$T_{vir} = 3.6 \times 10^5 \left( \frac{\sigma}{100 \text{ km/s}} \right)^2 \quad (9)$$

- Velocity dispersion of galaxies in group is smaller so temperature between groups is lesser than clusters.